

Utah State University
Department of Civil and Environmental Engineering
CEE 6400 Physical Hydrology

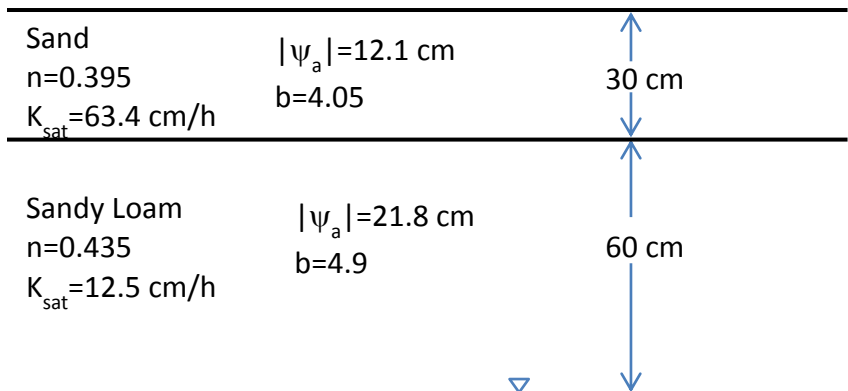
Final exam.
D.G. Tarboton

Date: 12/14/2011
Time: 110 min

[90 points open book portion. 120 points total]

Open Book. Answer all questions. Please answer on separate sheets of paper. You may refer to the textbook, notes, solutions to homework and any other written or printed reference material. Calculator use. You may use a programmable calculator or equivalent calculating device (e.g. calculator functionality on a phone). You should limit the use of the calculating device to the performance of calculations. You may use programs that you have written to evaluate quantities commonly used in this class (e.g. saturation vapor pressure). You may not use your calculating device to retrieve stored reference material in any form. You may not send messages or access the internet or communicate in any way with anyone other than the instructor or moderator regarding solutions to these questions.

1. **Water in Soil.** Consider two soils layered in the unsaturated zone under hydrostatic equilibrium. The water table is located at the bottom of the second layer.



The parameters indicated are Clapp and Hornberger (1978) parameters from Table 1, page 4:18 of the Rainfall Runoff Processes workbook.

- a. Plot the pressure head (matric potential) versus depth through the soil. [5]
- b. Indicate the height of the top of the capillary fringe. [5]
- c. Plot the water content versus depth through the soil. Indicate numerical values at the water table, top of capillary fringe, interface between soil types and surface. [5]
- d. Calculate the soil moisture deficit (cm). [5]

Assume a rainstorm during which 8 cm falls steadily during 1 day.

- e. Calculate the time to ponding. [5]
- f. Calculate the depth of runoff generated. [5]

[30 points]

2. **Evaporation by Penman-Monteith.** Consider a coniferous forest with the following information:

Dry gas constant, $R_a = 287 \text{ J kg}^{-1} \text{ K}^{-1}$	Incoming solar radiation, $K_{in} = 25 \text{ MJ m}^{-2} \text{ day}^{-1}$
Latent heat of vaporization, $\lambda_v = 2.46 \text{ MJ kg}^{-1}$	Net longwave radiation, $L = -5 \text{ MJ m}^{-2} \text{ day}^{-1}$
Density of water, $\rho_w = 1000 \text{ kg m}^{-3}$	Albedo, $a = 0.14$
Air heat capacity at constant pressure, $c_a = 1.005 \times 10^3 \text{ MJ kg}^{-1} \text{ K}^{-1}$	Maximum leaf conductance $C_{leaf}^* = 5.3 \text{ mm s}^{-1}$
Air density, $\rho_a = 1.13 \text{ kg m}^{-3}$	Leaf area index (LAI) = 6
Atmospheric pressure, $P = 95 \text{ kPa}$	$z_{veg} = 25 \text{ m}$
Air temperature, $T_a = 18 \text{ }^\circ\text{C}$	Shelter factor, $f_s = 0.5$
Relative humidity, $W_a = 0.54$	Soil moisture deficit, $\Delta\theta = 5 \text{ cm}$
Wind speed, $v_a = 3 \text{ m s}^{-1}$ at height $z_m = 2 \text{ m}$ above the top of the vegetation	

PenMontX.xls spreadsheet

Vegetation Type, Season:	$z_{veg} =$	25	m		
	$f_s =$	0.5			
	$C_{leaf}^* =$	5.30	mm/s	Table 7-5, Fig 7-14	
	$a =$	0.14		See Table 7-5	
	$LAI =$	6.0		See Table 7-5	
Weather, Soil:	$P =$	95	kPa		
	clear-sky solar radiation, $K_{cs} =$	25	MJ/m ² day;	See SolarRad.xls	
	cloud cover, $C =$	0	0 ≤ C ≤ 1		
	$T_a =$	18	C		
	$W_a =$	0.54			
	$v_a =$	3	m/s		
	$\Delta\theta =$	5	cm		
$\rho_w =$	1000	kg/m ³	$ea =$		kPa
$\rho_a =$	1.13	kg/m ³	$K_{in} =$	25.00	MJ/m ² day; Eqn. (7-26)
$\lambda_v =$	2.46	MJ/kg	$\epsilon_{at} =$	0.78	Eqn. (7-30)
$K+L =$	16.50	MJ/m ² day	$L =$	-5.00	MJ/m ² day
$e^*a =$		kPa	$\Delta ea =$		kPa
$\Delta =$	0.130	kPa/K	$\Delta\rho_v =$		kg/m ³
$\gamma =$	0.062	kPa/K			
$f(K_{in}) =$	0.812		$f(\Delta\rho_v) =$	0.528	
$f(T_a) =$	1.000		$f(\Delta\theta) =$	0.932	
	$f(K_{in}) * f(\Delta\rho_v) * f(T_a) * f(\Delta\theta) =$	0.399			
$C_{at} =$	2.69E+02	mm/s	$C_{leaf} =$		mm/s
			$C_{can} =$	6.34E+00	mm/s
	Penman-Monteith ET rate =		mm/s	=	
					mm/day

Refer to the Penman-Monteith equation in Dingman on page 299 and the PenMontX.xls spreadsheet given on the previous page that you used in your homework. Some of the cells have been blanked out

- a. Evaluate the saturation vapor pressure [5]
 - b. Evaluate the absolute humidity deficit $\Delta\rho_v$ [5]
 - c. Validate the value for $f_p(\Delta\rho_v)$ shown in the spreadsheet [5]
 - d. Evaluate the Leaf Conductance C_{leaf} [5]
 - e. Evaluate ET (mm/day) using the Penman-Monteith equation [10]
- [30 points]

3. **Infiltration and Runoff Generation.** Consider the following storm

Time (h)	0-2	2-4
Rainfall Intensity (cm/h)	0.5	2

Philip's equation is applicable with $K_p = 0.2$ cm/h and $S_p = 3$ cm/h^{0.5}

- a. Plot a graph of infiltration capacity as a function of infiltrated depth for this soil [10]
 - b. What is the time that ponding first occurs in this storm [10]
 - c. Determine the infiltration and runoff generated in each two hour increment [10]
- [30 points]