ABSTRACT: River channel geometry is an important input to hydraulic and hydrologic models. Traditional approaches to quantify river geometry have involved surveyed river cross-sections, which are complex to extend to ungauged basins. In this paper, we describe a method for developing a synthetic rating curve relating flow to water level in a stream reach based on reach-averaged channel geometry properties developed using the Height Above Nearest Drainage (HAND) method. HAND uses a digital elevation model of the landscape and computes the elevation difference between each land surface cell and the stream bed cell to which it drains. Taking increments in water level in the stream, HAND defines the inundation zone and a water depth grid within this zone, and the channel characteristics are defined from this water depth grid. We evaluate an application of our method on the Blanco River (TX) using 10-meter terrain data from the USGS 3DEP Elevation dataset. We compare the reach-average stage-river geometry relationships and rating curves to those from calibrated HEC-RAS models. The results demonstrate that after some adjustment, the river geometry information and rating curves derived from HAND using national-coverage datasets are comparable to those applied in local hydraulic models, built using more data intensive traditional cross section analysis.

KEY TERMS: hydrologic terrain analysis; river geometry; rating curve; HAND; flooding

INTRODUCTION

Flooding is the most threatening natural disaster worldwide considering the fatalities and property damage it causes. It makes up about 40% of all natural disasters worldwide and causes about half of all natural hazard fatalities (Noji, 1991; Ohl et al., 2001). Under a changing climate, the magnitude (Knox, 1993) and frequency (Milly, 2002) of floods may increase significantly, which, together with growing population and expanding urbanization, results in more serious and frequent flood hazards. For the 136 coastal cities across the world alone, the annual losses due to flooding have been projected to increase to $52 billion per year by 2050 (the 2005 estimate was $6 billion) considering socio-economic impacts alone, and this number could even reach $1 trillion if other factors are considered (Hallegatte et al., 2013).

Inundation maps show the spatial extent of flooding and play an important role in emergency response during flood events (Apel et al., 2009; Maidment, 2016). Accurately mapping flood inundation extent requires a comprehensive description of the geometry of the channel and floodplain, since flooding water is routed by the river fluvial system (Maidment, 1992). Traditional approaches to quantifying river geometry rely on measurements of river cross sections. Attempts to combine many independently developed local HEC-RAS models have failed due to variations in model development, overlaps in cross sections from one local model to another, and gaps in coverage of some streams (Zheng, 2015).

Other approaches to obtaining channel geometry without introducing cross sectional information have also been investigated, such as hydraulic geometry relationships (Leopold et al., 1953), and remotely sensed imagery inference (Pavelsky and Smith, 2008). Andreadis et al., (2013) developed a simple global river bankfull width and depth database using a regression relationship between bankfull discharge, drainage area and hydraulic geometry characteristics. Yamazaki et al., (2014) applied an algorithm that calculates the distance from remotely-sensed water body edge to the river centerlines following flow directions, to produce the Global Width Database for Large Rivers (GWD-LR) using the SRTM Water Body Database and the HydroSHED (Hydrological data and maps based on SHuttle Elevation Derivatives at multiple scales).
flow direction raster. Both bankfull width and effective river width without islands were computed for river channels between 60S and 60N (Yamazaki et al., 2014).

A so-called first fine-resolution, continental-scale river centerline and width database, the Landsat-derived North American River Width (NARWidth) dataset, has been developed (Allen and Pavelsky, 2015). It includes rivers ranging from approximately fourth to tenth Strahler stream order, the width of which are wider than 30 meter at annual mean discharge. Some limitations are found in these river geometry datasets: first, the resolution of the river network is not high enough to use in flooding studies of local streams. Taking Texas as an example, there are 20,004 HydroSHEDS flowlines in Texas, while the number of flowlines is 101,240 in the medium-resolution National Hydrograph Dataset Plus (NHDPlus) used in the National Water Model. Therefore, numerous local streams, which are critical during flood events, are not detected in the existing global river width and depth database. Second, only the bankfull width and depth are provided instead of a continuous relationship between stage height and channel properties, which limits the applicability of this dataset for inundation mapping.

While prior research using remotely sensed data or statistical approaches to investigate river geometry and rating curve has resulted in useful insights and general laws (Getirana et al., 2013; Paris et al., 2016; Garambois et al., 2017), these methods do not extract information from the actual terrain. General laws obtained from statistical analyses are thus insufficient to depict the unique physiographic characteristics of each channel, and remotely-sensed imagery only captures part of a transient state of the river system from a top view, which is incomplete. Therefore, a new approach is needed to take advantage of the available terrain information and provide channel characteristics for ungauged basins.

This paper evaluates a new method that estimates channel geometry properties and rating curves from high-resolution terrain data. This method uses hydrological terrain analysis to determine the Height Above Nearest Drainage (HAND) (Rodda, 2005; Renno et al., 2008), which is defined as the height of each grid cell with respect to the nearest stream cell it drains to. The HAND value of each grid cell thus indicates the water height
at which that cell is inundated. The inundated extent corresponding to a given water level may then be determined by selecting all the cells with a HAND value less than or equal to the given level. The water depth at each cell can then be computed using the water level minus its HAND value. The applicability of HAND to inundation mapping has been demonstrated in several studies (Rodda, 2005, Nobre et al., 2016). However, its application in describing river geometry information and retrieving stage-discharge relationship has not been explored. What hydraulic simulation really needs about river geometry is not the actual channel shape but the hydraulic parameters derived from the channel shape that are then used in the mass and momentum conservation equations. Hence, if the relationships between channel hydraulic parameters and stage height can be directly derived from hydrological terrain analysis products, as suggested by the results of the work here presented, inundation mapping can be performed with an alternative approach that does not rely on cross sectional information and hydraulic models (e.g. HEC-RAS).

This paper is organized as follows. Section 2 describes the workflow for the proposed approach: creation of HAND raster, evaluation of reach hydraulic properties and rating curves, and validation of the results. Section 3 presents a case study on the Blanco River (TX), and the comparison to a calibrated local HEC-RAS model. We discuss the results and remaining challenges in Section 4. Finally, concluding remarks are presented in Section 5.

METHODS

Our method contains three parts. The first part is a hydrologic terrain analysis workflow, which is modified from the original HAND model (Renno et al., 2008), to compute the HAND raster for the NHDPlus river network. In the second part, using the calculated HAND raster, we derive hydraulic properties for all the reaches in the river network. In the third part, we take these hydraulic geometry data and create a synthetic rating curve using Manning’s equation for each reach. Following these steps, we evaluate the validity of the terrain dataset for describing channel geometric details, and compare HAND-derived results to channel geometry and rating curves derived from local HEC-RAS models.
Hydrologic Terrain Analysis

The Height Above Nearest Drainage (HAND), first introduced by Rennó et al. (2008), is a special case of a hydrologic terrain proximity measure (Tesfa et al., 2011). There are multiple approaches to represent topography-driven flow over a terrain represented by a digital elevation model (DEM). The $D8$ model (O'Callaghan et al., 1984) assigns a single flow direction from each grid cell to one of its neighbors based on the steepest descent direction. It is the earliest and simplest method developed, and is still widely used due to its simplicity and the property that flow does not diverge, which is desirable when mapping stream flow paths. The $D\infty$ model introduced by Tarboton (1997) generalizes $D8$ by representing flow direction as a vector along the direction of steepest downward slope on one of the eight triangular facets centered at each grid cell. Flow from a grid cell is shared between the two down slope grid cells closest to the vector flow angle based on angle proportioning (Fig.1). Taking the advantage of the $D\infty$ flow model, Tesfa et al. (2011) developed methods to derive a wide range of flow related quantities useful to hydrological and environmental modeling, including the calculation of distance to stream (horizontal or vertical). The TauDEM software (Tarboton, 2016) implements these methods. In this paper we use the $D\infty$ approach for the computation of HAND as the vertical distance or drop to a stream (Fig. 2) as implemented in the TauDEM software.
FIGURE 1: The $D_8$ and $D_\infty$ Flow Models (figure reproduced from Tesfa et al., 2011).

FIGURE 2: Definition of proximity measures defined by Tesfa et al., (2011) for distances up (to ridge) and down to stream. HAND is evaluated using $v_s$, the vertical drop to stream (figure reproduced from Tesfa et al. (2011))

The vertical drop to a stream (HAND value) is computed as:
\[ h(i) = \frac{\sum P_{ik}(drop(i,k) + h(k))}{\sum P_{ik}} \]  \hspace{1cm} (1)

where \( P_{ik} \) is the proportion of grid cell \( i \) that drains to grid cell \( k \), \( h \) is the vertical drop from a grid cell to the stream and \( drop(i,k) \) the drop (change in elevation) from grid cell \( i \) to \( k \) defined as:

\[ drop(i,k) = z(i) - z(k) \]  \hspace{1cm} (2)

where \( z \) represents the elevation values at grid cells \( i \) and \( k \). In Equation (1) the sum is over the grid cells for which \( P_{ik} \) is greater than 0 and for which \( h(k) \) exists. The denominator in (1) is used to normalize for flow paths that leave the domain without reaching a designated end point grid cell (there is an option implemented in the code (Tarboton, 2016) to report no data rather than use this normalization). Tesfa et al. (2011) present this function as one option within a general distance to target set function where \( drop(i,k) \) may be replaced by a general distance measure computed in any number of ways (e.g. horizontally, vertically or along the slope). Note that drop to stream expressed in these equations is defined recursively with the drop from any grid cell as the weighted average of the drop from downslope cells, using cell to cell flow proportions as weights. The result is thus a form of weighted average along all the flow paths from a cell to the stream. The computation is initiated by setting the distances to 0 for all stream cells, and then enabling the evaluation of \( vs \) (i.e. HAND) for cells for which all downslope quantities in the domain have been evaluated. Grid cells where all downslope values are available are placed on a computational queue. To enable parallel computation, the domain is decomposed into partitions, and a queue maintained for separate processes operating on each partition. Computational details are given in Tesfa et al. (2011).

The \( D8 \) approach with weighted average distance to the stream is used here as it provides a smoothing of the HAND values, effectively averaging sharp HAND differences between adjacent grid cells that may drain to stream cells of different elevation resulting from the \( D8 \) approach. This approach appears to better represent the spreading out of water over the terrain when HAND is used to evaluate flood inundation and channel hydraulic properties.

A prerequisite for evaluating HAND is a raster representation of the stream
network. These are stream grid cells where HAND is assigned to be 0. The TauDEM $D^\infty$ distance down function may actually be evaluated for any target zone represented by a set of grid cells to which the distance is to be computed for whatever purpose. However, in the evaluation of HAND, the target zone is a raster representation of the stream network. There are many approaches to the definition of a raster stream network based on DEM flow models. These generally use the $D8$ method, as defining divergent stream networks is impractical. TauDEM implements a number of the methods described by Tarboton and Ames (2001; Tarboton et al., 1992; Tarboton et al., 1991), including simple contributing area threshold methods, and more advanced methods based on measures of curvature to identify valley grid cells, objectively adapt to the complexity of the topography, and quantify drainage density.

In this paper, our interest is in stream networks aligned with the NHDPlus dataset used by the National Water Model. The NHDPlus stream network was mapped at a nominal 1:100,000 resolution. The USGS National Elevation Dataset (NED) DEM is currently available at a 1/3 arc sec (~10 m) horizontal resolution across the continental US and represents information at a finer resolution more consistent with 1:24,000 scale mapping.

NHDPlus streams, however, do not always align with valleys in the 1/3 arc sec NED DEM. To avoid the spurious HAND values that would result from calculating HAND to a direct rasterization of NHDPlus flowlines, we derived a stream raster at the same drainage density as the NHDPlus stream network, but aligned with 1/3 arc sec NED DEM. This operation was performed by identifying the upstream channel head of each first order NHDPlus stream and representing this as a grid cell with value of 1, and setting all other grid cells to a value of 0 in a stream source weight grid. This weight grid was then used as input to a weighted flow accumulation calculation using $D8$ flow directions (TauDEM areaD8 function). Stream grid cells were mapped where the weighted flow accumulation was greater than 1. The result is a raster representation of a stream network originating at each source point, but following down the valleys as indicated in the 1/3 arc sec DEM (Fig. 3). This stream raster was used as the target set in the evaluation of vertical distance down using the TauDEM distance down function to obtain HAND values (Fig. 4).
FIGURE 3: Stream raster derived from channel head sources of NHDPlus medium resolution streams. The red grid cell is the channel head source grid cell. Blue grid cells are the stream raster evaluated as a weighted flow accumulation of these red grid cells. The black line is NHDPlus stream. The lines are overlaid on elevation contoured with a 2 m interval. The horizontal offset between the NHDPlus streams and the valleys as depicted by contours from 1/3 arc sec NED DEM is corrected in the stream raster.
FIGURE 4: Height Above Nearest Drainage (HAND) evaluated on 1/3 arc sec NED DEM relative to a stream raster derived from NHDPlus medium resolution stream network source grid cells. 2 m terrain contour interval drawn as background.

Implementation of the above methods requires a DEM that is hydrologically conditioned, or has had the pits removed so that each grid cell can drain to the edge of the domain, or to an identified internally draining sink along a flow path that is not increasing. In this work, the TauDEM pitremove function was used to hydrologically condition the DEM prior to the analysis.

The complete set of hydrologic terrain analysis processing steps is:

1. Fill pits using TauDEM pitremove function.
2. Calculate $D8$ flow directions using TauDEM d8flowdir function.
3. Calculate $D\infty$ flow directions using TauDEM d8flowdir function.
4. Define channel head source grid cells from NHDPlus streams.
5. Calculate the weighted flow accumulation using channel head grid cells as input to TauDEM $D8$ contributing area function.
6. Define the stream raster using a threshold of 1 with weighted flow accumulation.

7. Calculate HAND using $D_{\infty}$ distance to stream function with the vertical drop option.

River Geometry and Rating Curve Estimation

The conceptual basis for implementing HAND in inundation mapping is as follows. A river segment is defined as a stream reach $R$. The reach catchment, $C$, contributes the local drainage area of the stream reach $R$. Let us define the value, $L$, as the length of the reach $R$ measured along its thalweg line. A measure location, $m$, along reach $R$ is defined by its percentage distance from the lower end of the reach, in other words by the ratio of the length from that location to the lower end of the reach, divided by the length of the reach, $L$. The water level, $y$, at any location $m$ along the stream channel is given by the difference between the water surface elevation and the minimum channel elevation at that location, designated by $y(m)$. The average water level along the stream reach is given by $y$. The HAND value, $h(s)$, is the elevation difference between a cell, $s$, on the land surface within the reach catchment, and the minimum channel elevation at the location on the corresponding stream reach where water draining from that cell converges into the channel. The location, $s$, on the land surface is inundated if the water level in the channel reach is greater than the HAND value of that location, i.e. inundation occurs if $y > h(s)$.

The conceptual basis for implementing HAND to estimate the channel hydraulic properties (Fig. 5) and rating curve is as follows: for reach $R$ at a water level of $y$, all the cells, $s$, with a HAND value smaller than $y$ compose an inundated zone $F(y)$, which is a subarea of the reach catchment $C$. The water depth at any cell $s$ in the inundated zone, $d(s)$, is the difference between the reach-average water level $y$ and the HAND of that cell $h(s)$, which can be represented as:

$$d(s, y) = y - h(s), s \in F(y)$$  \hspace{1cm} (3)

Since a uniform reach-average water level $y$ is applied to check the inundation of any cell within the catchment, the inundated zone $F(y)$ should be interpreted at reach level.
The water surface area of the inundated zone at a water depth of \( y \), \( S(y) \), can be calculated as:

\[
S(y) = \sum_{s \in F(y)} A(s) \tag{4}
\]

where \( A(s) \) is the area of cell \( s \).

The channel bed area of the inundated zone at a water depth of \( y \), \( B(y) \), can be calculated as:

\[
B(y) = \sum_{s \in F(y)} A(s) \sqrt{1 + \text{slp}(s)^2} \tag{5}
\]

where \( \text{slp}(s) \) is the surface slope of cell \( s \), expressed as rise/run or \( \tan \) of the slope angle. This equation approximates the surface area of the grid cell as the area of the planar surface with surface slope, which intersects with the horizontal projected area of the grid cell.

The flood volume of the inundated zone \( V(y) \) at a water depth of \( y \) can be calculated as:

\[
V(y) = \sum_{s \in F(y)} A(s) \cdot d(s, y) \tag{6}
\]

If the reach length \( L \) is known, the reach-average channel width at a water depth of \( y \), \( W(y) \), can be calculated as:

\[
W(y) = S(y)/L \tag{7}
\]

Similarly for the reach-average cross section area \( A(y) \):

\[
A(y) = V(y)/L \tag{8}
\]

and the reach-average cross section wetted perimeter \( P(y) \):

\[
P(y) = B(y)/L \tag{9}
\]

Combining the reach-average cross sectional area \( A(y) \) and the wetted perimeter \( P(y) \) gives the reach-average cross section hydraulic radius \( R(y) \) as:

\[
R(y) = A(y)/P(y) \tag{10}
\]

If the channel bed slope of reach \( R \) is \( S \) and a Manning’s value is assumed as \( n \), the Manning’s equation can be applied to obtain a discharge \( Q(y) \) corresponding to the water depth of \( y \) at uniform flow as:
Computing the discharge \( Q(y) \) for different water depth \( y \) results in a synthetic rating curve for reach \( R \). This rating curve relates the average water depth to the discharge in the reach \( y(Q) \), where the discharge is assumed to be uniform along the reach. Therefore, this synthetic rating curve can be used as a tool to convert forecast discharges generated by large scale hydrologic models into corresponding water depths.

We implement this conceptual framework in the continental U.S with the 1/3 arc sec (10-meter) USGS 3DEP Elevation dataset and the NHDPlus dataset (Liu et al., 2017). The reach length and channel bed slope come from the attribute table of the flowline feature class in the NHDPlus dataset. By conducting these computational steps, a new continental-coverage high-resolution channel property dataset can be obtained for the continental U.S., indexed by the NHDPlus Common Identifier (ComId), and can be used to support future continental river dynamics research.

### Integrity Checking of River Geometry and Rating Curves

The river channel geometries and synthetic rating curves defined using HAND are averages over the length of a channel reach derived by slicing the terrain surface longitudinally along the channel flow path, rather than transversely to the flow path, at intervals to form individual cross-sections, as is traditionally done in one dimensional river hydraulic models. One way of checking the integrity of the HAND-derived information is to compare the results with those derived from a HEC-RAS model of the same river. Several comparisons are needed: (i) the minimum channel elevation, (ii) the stream geometries, and (iii) the synthetic rating curves.

\[
Q(y) = \left( \frac{1.00}{n} \right) \frac{2}{AR^2S^2} \tag{11}
\]
The minimum channel elevation at a particular measure location \( m \), \( z_c(m) \), is the elevation above geodetic datum of the stream thalweg at that location. When a stream is represented by a sequence of cells in a DEM, the DEM cell that corresponds to location \( m \) has a DEM channel elevation above geodetic datum of \( z_d(m) \). Because digital elevation models are smoothed versions of land surface topography, and because the digital elevation model may have been created when the channel was partly filled with water, the DEM channel elevation is generally higher than the minimum channel elevation. The value \( \Delta z(m) = z_d(m) - z_c(m) \) represents the bed elevation difference between the DEM channel elevation and the thalweg channel elevation at that location. The mean value of this bed elevation difference along a stream reach is given by \( \Delta z \).

An assumption of our implementation that needs to be evaluated is whether a DEM at a resolution of 10 meters is able to capture the terrain details within the channel. One way of carrying out this evaluation is to compare the streamline bed elevation profile extracted from the 10-m DEM, with the minimum channel elevation in a HEC-RAS model obtained by connecting the minimum elevation of HEC-RAS cross sections from upstream to downstream. In order to keep the same profile length and elevation sampling rate in the two methods, we adopt the streamline measure system of the HEC-RAS model, and obtain the DEM-derived profile by intersecting the DEM-derived flowline with the HEC-RAS cross sections and extracting the DEM elevations of the intersected locations.

Because \( \Delta z \) is generally greater than zero, it is useful to introduce a bottom shift into the HAND-derived water levels reflecting the “shelf effect” where the bottom of a DEM channel is actually flat over a finite area. Using this approach, the channel width \( W \) is a positive number when the water level \( y \) is zero, so the true water depth is larger than that computed using the DEM alone.

HAND-derived channel hydraulic properties can also be compared with those derived from river geometry information stored in HEC-RAS models. The main channel property that we evaluated was the channel width, because it is a description of the river geometry that is readily obtained by the HAND method. To do this, we derive a water level-channel width relationship from the HAND raster for a river segment using Eq. (7). Since the cross section shape is stored in HEC-RAS, a similar relationship can be established from the shape of each cross section located on the study reach. These cross
section level-width relationships form a sample space for a given stream reach. If the HAND-derived relationship falls within this sample space, we have some confidence that the accuracy of the HAND-derived river geometry information is comparable to that of the river geometry data used in local hydraulic simulations. Taking the channel widths for all the cross sections on the segment at the same water level, together with the distance between adjacent cross sections, we can compute the flood volume corresponding to the given water depth. If the volume is divided by the total length of the segment, an equivalent reach-averaged channel width can be derived from these cross sectional shapes. Repeating this process for a series of threshold water depths gives us a reach-averaged water level-width relationship derived from cross sectional shapes. Calculating the difference between this cross section-derived relationship and the HAND-derived relationship also helps to evaluate the quality of HAND-derived river geometry information.

A third part component of the integrity checking is to compare the HAND-derived rating curves with the rating curves stored in local HEC-RAS models. If a HEC-RAS project contains the simulation at multiple flow conditions, a rating curve will be generated for each cross section from the steady flow simulation results. Similar to the channel width sample space we use to validate river geometry, a rating curve sample space for the river segment is established from rating curves from different cross sections. To better quantify the water depth uncertainty brought by channel geometry, a fixed flow rate is assigned to every cross section in a HEC-RAS model for a given channel reach to create a representative flow condition that is replicated with the HAND-derived rating curve. In this way, the water depth uncertainty caused by the difference in discharge between HAND and HEC-RAS is eliminated. This median rating curve in the rating curve sample space from HEC-RAS is chosen as the reference to validate the HAND-derived rating curves. The optimal roughness value is selected for the HAND-derived rating curve by minimizing the root-mean-square error (RMSE) between the HAND-derived rating curve and the median rating curve from HEC-RAS.
APPLICATION OF THE PROPOSED APPROACH

Study Area and Data

In order to evaluate our approach, we conduct a case study on the Blanco River (Fig. 6) following the steps described in the Methods section. The Blanco River is located in Central Texas, which is one of the most flash-flood prone regions in North America. In May 2015, a historic flash flood occurred across parts of Central Texas, causing severe life and property losses. The Blanco River was one of the most affected areas in this flood due to a flood wave of more than 12 meters in water depth.

The network of the Blanco River watershed is composed of 170 medium-resolution NHDPlus reaches. The total drainage area is 1129.57 km², and the average drainage area of the individual reach catchments is 6.72 km². The total river length is 539.71 km, and the average river length of the reaches is 3.17 km. For the hydrological terrain analysis portion, we created the HAND raster for the Blanco watershed. The DEM used in this study is the 1/3 arc-second DEM from the USGS 3DEP Elevation dataset with horizontal resolution of about 10 meters. The RMSE is 1.55 meters and represents the vertical accuracy of the DEM (Gesch et al., 2014). A calibrated HEC-RAS steady flow model, covering the lower half of the Blanco River main channel, was provided by the Fort Worth District of the U.S. Army Corps of Engineers and used as the reference for river geometry and rating curve comparison. In particular, we implemented the approach for a single NHDPlus reach with COMID 1630223. We chose this reach because: (1) its length is close to the average river length of the entire NHDPlus network with 2.67 million reaches, making it a representative reach for the catchment; (2) the reach is covered by the local HEC-RAS model and there are 8 cross sections lying on this reach; (3) the reach is close to Wimberley where 11 people were killed in the 2015 Memorial Day Flood, adding practical significance to understanding this reach.
The eight HEC-RAS cross sections are also shown in Figure 6. The main channel Manning’s $n$ value is 0.045 for all the cross sections, while the floodplain Manning’s $n$ varies from 0.06 to 0.1. The Manning’s $n$ values applied in the HEC-RAS model provide a proper range for roughness adoption when the depth-discharge relationship (rating curve) is established through HAND.

**Hydrologic Terrain Analysis**

A 10-meter HAND raster (Figure 7) was generated for the Blanco River watershed based on the 10-m resolution DEM raster and the 10-meter river network raster initiated at NHDPlus stream sources. While the original DEM has elevations that range from 165 meters to 618 meters, a difference of 453 meters, the HAND raster ranges from 0 to 161 meters. This difference in elevation range reflects that HAND measures
only the relief relative to streams.

In addition, since the HAND raster is built upon flow directions, derived from a hydrologically conditioned DEM, it forms a continuous surface across the whole domain. This continuity brings two advantages to the HAND method over the planar linear interpolation approach used for inundation mapping based on cross sections (Apel et al., 2009): (1) local depressions that are never connected to the flow can be avoided; (2) the mass conservation law can be adhered to.

![FIGURE 7: DEM and HAND for Blanco Watershed](image)

Figure 8 illustrates the stream network and NHDPlus channel heads used to define the stream network raster for the Blanco Watershed. The blue polylines are from the NHDPlus flowline feature class. A geoprocessing tool was used to identify the channel heads of all the first-order reaches. The cells on the flowpaths starting from these channel heads following the $D8$ flow directions were identified as stream cells. Although the majority of the DEM-derived flowlines line up with the NHDPlus flowline features, the
advantage of adopting DEM-derived flowlines instead of NHDPlus flowlines is that it guarantees that the streams pass through the valley portion of the digital terrain dataset.

FIGURE 8: Stream Definition in HAND.
River Geometry and Rating Curve Estimation

By setting a water level threshold to the HAND raster, the inundation extent consisting of all the cells with a HAND value smaller than the threshold, can be generated. The water depth raster is then computed by using the threshold water level value subtracted from the HAND value (Eq. (3)). All the inundated cells have a positive water depth, and the stream cells have a water depth equal to the threshold water level.

The procedure for obtaining river geometry properties for each reach is illustrated here for the selected study reach and catchment (COMID: 1630223). We first clip the Blanco watershed HAND raster with the catchment boundary polygon to obtain a HAND subset for that catchment. From the HAND raster, we create the water depth grids that correspond to a series of threshold water levels from 0 to 18.29 meters (60 feet) at an interval of 0.3048 meter (1 foot). As shown in Figure 9, water spreads out of the channel and the depth at the same location increases as the water level rises up. Following the method described earlier, we get the water level-channel geometric property relationships for this reach as shown in Table 1.

To estimate the rating curve for that reach, the derived water level-cross sectional area and water level-hydraulic radius relationships, together with the river length and reach average slope attributes of that specific reach from the NHDPlus dataset and Manning's roughness coefficient, are substituted into the Manning’s flow resistance equation. In this study for Reach 1630223, the segment length is 2.055 kilometers, and the channel bed slope is 0.001976. Manning’s $n$ value was taken as 0.05 for consistency with the HEC-RAS model for this river. Selection of Manning’s $n$ is a source of uncertainty in this approach and its calibration is discussed in the validation section.
FIGURE 9: Water depth grids at different water levels (0, 3.05, 6.10, and 9.14 meters).

Table 1: HAND-derived river geometry parameters and rating curve for reach 1630223.

<table>
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<tr>
<th>Water Level (m)</th>
<th>Number of Inundated Cells</th>
<th>Water Surface Area ($10^4$ m²)</th>
<th>Channel Bed Area ($10^4$ m²)</th>
<th>Flood Volume ($10^4$ m³)</th>
<th>Channel Width (m)</th>
<th>Wetted Perimeter (m)</th>
<th>Wet Area (m²)</th>
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Theoretically, when water level equals to zero, the channel is represented by a thalweg line with a width of zero. However, from Figure 9(a) and the zero depth row in
Table 1, we can see that there is a bottom width of 38 meters in HAND-derived river geometry, which means HAND-derived river geometry is not able to reach down to the level of the thalweg. Therefore, a shift must be made to the bottom of the HAND-derived river geometry information.

**River Geometry and Rating Curve Validation versus HEC-RAS**

To evaluate the 10-meter terrain dataset used to estimate river geometry, a streamline profile comparison was conducted for the whole modelled river segment and the single reach 1630223. For the profile comparison of reach 1630223 (shown in Figure 10(a)), the DEM-derived profile is 0.13 meter higher than the HEC-RAS profile on average with a standard deviation of 0.12 meter. The profile derived from the pit-removed DEM, which is the actual one used in HAND computation, is 0.88 meter higher than the HEC-RAS profile on average, with a standard deviation of 0.95 meter. The results show that for this reach, the 10-meter DEM is very close to the thalweg, but the pit filling process introduces an extra bias to the accuracy of the terrain dataset, and affects the accuracy of the HAND results. The same comparison is repeated for the entire profile across the modelled channel shown as Figure 10(b) and the same conclusion can be drawn. For the entire 82-kilometer modelled segment, the DEM-derived profile is 0.49 meter higher than the HEC-RAS profile on average with a standard deviation of 1.23 meter; the profile derived from the pit-removed DEM is 0.99 meter higher than the HEC-RAS profile on average with a standard deviation of 1.26 meters.
FIGURE 6: Comparison between the minimum channel elevation profiles from the DEM, the pit-filled DEM, and HEC-RAS streamline profile comparison.

To validate the HAND-derived river geometry, we derived a water level-channel width relationship for each cross section and a reach-average relationship, depending on cross sectional shapes and distances. These relationships compose the validation reference (shown by the dotted red line in Figure 11) derived from the HEC-RAS model. According to Table 1, when the water depth is zero, a corresponding channel width of 38-meter is derived from the HAND raster for reach 1630223. From Figure 11, a depth of 0.64 meter is interpolated on the reach-average water level-width relationship for a 38-meter channel width. This depth is treated as the bottom shift needed to adjust HAND-derived river geometry in this reach due to the limitation caused by the terrain dataset resolution. After the adjustment is made, the comparison between HAND-derived depth-width relationship and HEC-RAS-derived depth-width relationship is shown as Figure 11. As we can see, the HAND-derived depth-width relationship always falls in the sample space composed of individual cross section depth-width relationships. The RAS-derived reach-average channel width is 12.04 meter wider than the HAND-derived reach average width on is within the depth range from 0.92 meter (3 feet) to 15.24 meter (50 feet). The standard deviation of the width difference is 19.33 meters. If the difference is normalized with the RAS-derived reach-average channel width in that range, the relative mean difference is 3.2 percent, which demonstrates a good fit of the HAND-derived river geometry to the actual channel hydraulic condition.
FIGURE 7: Comparison between HAND-derived and RAS-derived depth-width relationships on r1630223.

To validate the rating curves derived with HAND, we conducted steady flow simulation with HEC-RAS under multiple flow conditions. In each cross section, the water level-discharge data pair under a single flow condition is a point on the rating curve of that cross section and the rating curves of all the cross sections in a reach compose the reference rating curve sample space. There are eight flow conditions (profiles) stored in the approved HEC-RAS model, which correspond to the 2-yr (232 m$^3$/s), 5-yr (736 m$^3$/s), 10-yr (1249 m$^3$/s), 25-yr (2067 m$^3$/s), 50-yr (2784 m$^3$/s), 100-yr (3568 m$^3$/s), 250-yr (4701 m$^3$/s), and 500-yr (5607 m$^3$/s) floods in the Blanco River. To better represent the depth-discharge relationship in low flow condition, we added six extra profiles. One of these profiles is the annual mean flow condition (2 m$^3$/s), which is stored as an attribute of every reach in the NHDPlus flowline attribute table. Another three profiles correspond to 20% (0.4 m$^3$/s), 50% (1 m$^3$/s) and 80% (1.6 m$^3$/s) mean annual flow. The last two profiles (79 m$^3$/s and 155 m$^3$/s) are obtained by linearly interpolating between the annual mean flow and the 2-yr flood. The downstream boundary condition of the steady flow simulation is set as the normal depth. Since we set a constant flow rate to all the cross
sections across the reach, for each flow condition, a box plot can be used to quantify the variability in stage across the cross sections due to shape differences and other hydraulic interactions. Connecting the median stage of each box plot produces a median rating curve. This median rating curve is applied to identify the corresponding discharge for the channel bottom missing in the HAND-derived river geometry and rating curve. For the depth shift of 0.64 m, the discharge added to the bottom of the HAND-derived rating curve is 22 m$^3$/s. Then the entire HAND-derived rating curve is shifted with a depth of 0.64m and a discharge of 22 m$^3$/s. Figure 12 shows the comparison between the HAND-derived rating curve (after shift) and the HEC-RAS rating curve sample space. The Manning’s $n$ roughness value used to build this rating curve is 0.05. Flow conditions larger than the minimum discharge in HAND-rating curve are used to quantify the fitness of HAND-derived rating curve and the reference median rating curve. Therefore, 10 of these 14 flow conditions are adopted. For those specific flow rates, corresponding stage heights are obtained from the HAND-derived rating curve and the HEC-RAS median rating curve. For the case with the Manning’s $n$ of 0.05, the water level read from the HAND-derived rating curve is 0.52 meter higher than the stage height read from the HEC-RAS median rating curve on average with a standard deviation of 0.09. If the difference is normalized using the median stage height, it represents a mean difference of 7.7 percent.
FIGURE 8: Comparison between HAND-derived and RAS-derived rating curves on reach 1630223 (n=0.05).

Next, the optimal roughness value is determined by minimizing the mean stage height difference in absolute value for the given flow conditions searching across Manning’s n values between 0.040 and 0.06 at an interval of 0.001. The variation of the mean stage height difference within this range is shown in Figure 13. The mean stage height difference absolute value is minimized to 0.02 meter at a Manning’s n of 0.043, which is slightly smaller than the channel roughness value used in the HEC-RAS model (0.045). This difference is inconsequential. If the actual 0.045 Manning’s n value is adopted, the mean difference is 0.17 meter, which is an acceptable conversion for inundation mapping purpose. The rating curve comparison with the Manning’s n of 0.045 is shown in Figure 14. The fact that the calibrated and HEC-RAS n values are close and the rating curves consistent, supports the finding that the HAND DEM analysis is a valid approach to determine hydraulic parameters and is expected to produce results comparable to the more data intensive HEC-RAS approach, which is difficult to apply at continental scale.
**FIGURE 9**: Relationship between Manning's n and the mean stage height difference absolute value.

**Figure 10**: Comparison between HAND-derived and RAS-derived rating curves on reach 1630223 (n=0.045).

**DISCUSSION**
This paper has presented a new method for the determination of reach average hydraulic properties from a digital elevation model based on the Height Above Nearest Drainage (HAND) approach. Any method is only as good as the data is and this approach relies on the fidelity with which the DEM represents the shape of the river channel. The comparison to HEC-RAS cross sections showed that the method can produce reasonable results. This holds promise, as the method can be fully automated and is based on readily available national data and can thus be applied rapidly across the whole country reducing the need for detailed cross section-based flood inundation mapping. We do acknowledge the preliminary and approximate nature of this method, particularly in areas where artificial hydraulic structures or momentum interaction between channel and floodplain controls the propagation of flood waves. Therefore, we suggest it be used primarily as a screening tool to identify locations where more detailed study is warranted. It also has the potential to support national scale modeling, such as the National Water Model. We did find, with the HEC-RAS comparisons, that adjustment of the base elevation may be needed in certain cases. We expect that as DEMs are improved, especially if and when they include channel bed bathymetry, perhaps from water penetrating LIDAR or sonic depth measurement, that the need for such adjustments will be reduced, and that the results from HAND will become better.

There are some DEM and hydrography considerations that need to be addressed in applying HAND. We illustrated how the pit filling process needed to ensure a hydrologically conditioned DEM where each grid cell drains to the edge of the domain, can result in inflated DEM values along the streams. Some of these values occur behind barriers due to artefacts in the DEM production process and due to the DEM representing the elevation of road/railway crossings and not the elevation of the bridge or drain beneath these crossings through which water passes. We are investigating ways to use high resolution hydrography information (e.g. NHD HR, nominally at 1:24,000 scale (ftp://rockyftp.cr.usgs.gov/vdelivery/Datasets/Staged/Hydrography/NHD/National/HighResolution/) that represents flow lines with greater fidelity than NHDPlus) to adjust the DEM so that elevation is non increasing along hydrographically mapped flow lines. This provides the capability to punch through barriers where the hydrography indicates that
flow crosses the barrier, partially alleviating this problem. We are also investigating using geodesic approaches to map flow paths (e.g., Passalacqua et al., 2010; Sangireddy et al., 2016) to overcome barriers more automatically using geomorphologically based filtering approaches without the requirement for hydrographic mapping.

We also showed how hydrography, notably the NHDplus medium resolution hydrography used in the National Water Model can be misaligned with valley paths in a DEM. The HAND approach follows flow directions downslope and requires streams aligned with the DEM. Using the NHDPlus flowlines directly would have resulted in spurious results for the area (as illustrated in Figures 3 and 4), and this motivated our use of the DEM stream delineation approach starting from NHDPlus channel heads. However, even with this approach, there is not a guarantee of a one to one mapping between stream segments in the DEM delineated network and NHDPlus, and areas draining to DEM stream segments may not align exactly with NHDPlus catchments resulting in some errors around the edges when we clip the HAND raster based on NHDPlus catchments. There is thus a need, in national datasets, for better alignment and reconciliation of elevation and hydrography representations of streams, through efforts such as NHDPlusHR (Viger et al., 2016).

The channel properties are currently organized by reach and a uniform water depth is assigned to a reach during the inundation mapping process. Sometimes reaches are quite long and assuming uniform depth is unreasonable. It is possible to split reaches into shorter segments, but we leave to future work the exploration of the best length to use when considering splitting reaches. The optimal distance between cross sections in 1D hydraulic modelling has been shown to be proportional to the bankfull width (Samuels, 1990; Castellarin, 2009); adding extra cross sections within the optimal spacing decreases rather than increases the accuracy of the simulation due to rounding errors (Castellarin, 2009). If the segments of a reach can be specified and exported during the HAND computational process, these new profiles across the stream cells have a potential to replace the traditional cross sections used in 1-D hydraulic models. Organizing hydraulic properties in a segment unit smaller than a reach also has the potential to help resolve the instability problem in large-scale hydraulic models when a sudden channel shape change happens at a river confluence. The validation of HAND
channel geometry properties through the comparison with HEC-RAS-derived reach-average channel should be extended to a larger sample size. To ensure comprehensiveness, this sample should cover reaches of different stream orders and with different physiographic settings.

A generic way to evaluate channel and floodplain roughness values from land cover information or any other instructive variables would be helpful to improve the accuracy of the HAND rating curves. If the bankfull depth information of all the rivers in a large-scale network could be derived from the geometry data, instead of applying a single Manning’s equation to all water levels in a reach, a compound uniform flow equation could be implemented to better describe the hydraulics when the water level reaches the floodplain with a different roughness value. Also, the hydraulic conductance underestimation problem of empirical hydraulic equations at high flow condition needs to be considered. If a large-scale hydrodynamic model such as SPRNT (Liu and Hodges, 2014) is used, rating curves can be generated from the dynamic simulation with HAND river geometry information fed to the model. Note that, if a different method is used to determine the water depth in the channel, such as by direct observation or by using a solution of the full Saint Venant equations (SPRNT), then the hydraulic geometry data and the HAND raster can be used to produce an inundation map without the need for use of a synthetic rating curve.

CONCLUSION

In this paper, a workflow for computing river geometry and estimating channel reach rating curves based on DEM derived Height Above Nearest Drainage (HAND) was presented. This was illustrated for NHDPlus reaches of the Blanco watershed using the 1/3 arc sec USGS 3DEP Elevation dataset DEM. The workflow requires as input only a DEM, channel heads (or a stream network from which they can be extracted), and a priori Manning's n. The hydraulic geometry properties and rating curve derived from the HAND approach were shown to be generally consistent with similar information derived from more traditional cross sections and HEC-RAS hydraulic modeling, in a much more labor and data intensive process. Issues related to DEM fidelity and the need for
adjustments in the base elevation were identified and discussed. Calibration, to determine an optimal Manning’s n roughness parameter produced a value very close to the value used in HEC-RAS modeling, further validating the approach. Overall, this approach was shown to have promise for supporting quantitative hydraulic modeling at continental scale using readily available national datasets. A companion paper (Liu et al., 2017) applies this approach to this nationally available data using high performance computing.

Recent flood disasters resulting from hurricanes Harvey, Irma and Maria, emphasize the need for rapid, approximate flood inundation mapping over very large areas. The authors were involved at the Texas State Operations Center in the flood emergency response for Hurricane Harvey in Texas, which produced flooding in about 40,000 miles of streams and rivers in Southeast Texas during August and September 2017. Hurricane Harvey alone was the worst recorded storm for 3-5 day duration rainfall in the history of the United States. This resulted in a huge flood emergency response operation involving hundreds of helicopters and aircraft, thousands of trucks and boats, and tens of thousands of flood emergency response personnel, directed from the Texas State Operations Center. A critical piece of information in facing such a huge disaster is a map of the flooded water conditions across the landscape throughout the impacted zone to inform the direction of flood emergency response to people and communities who need help.

During Hurricane Harvey, the US Army Corps of Engineers produced flood inundation mapping using engineering scale models on the main stem rivers of the region, including the Guadalupe, Colorado, Brazos, Trinity, Neches and Sabine rivers. The Height Above Nearest Drainage method linked to flows computed by the National Water Model was used to create inundation mapping throughout the region. To be effective in providing actionable intelligence for flood emergency response, such mapping is required within a few hours of the forecast discharges becoming available. There are many approximations inherent in the flood inundation mapping described in this paper. However, what the events during Hurricane Harvey demonstrated is that this method can be applied quickly to provide an estimate of the flood inundation extent over a very large region.
ACKNOWLEDGEMENTS

This research has been supported in part by Texas Division of Emergency Management under grant number 26-3215-2275 and Consortium of Universities for the Advancement of Hydrologic Science, Inc. (CUAHSI). Part of this study was conducted during the 2016 National Water Center Innovators Program: Summer Institute at the National Water Center. Thanks to Fort Worth District of US Army Corps of Engineers for providing the Blanco HEC-RAS model. Thanks to the Editor, Associate Editor, and three reviewers for insightful comments which significantly improved this work.

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